

Mathematical Methods for Thermal Stress Analysis of Multilayered Composite Gun Barrels: A brief review

B. B. Pandit *Department of Mathematics, Shri Datta Arts, Commerce and Science College, Hadgaon, Dist. Nanded, Maharashtra, India- 431712*

Email: panditbhagwat51@gmail.com

Abstract:

Multilayered composite gun barrels, which combine metallic and composite layers, offer significant advantages over traditional barrels. This design enhances strength-to-weight ratios, improves thermal management, and increases corrosion resistance. However, the complex interaction of high temperatures, steep thermal gradients, and material property differences during firing requires a thorough understanding of the thermal stresses generated within these structures. These stresses can lead to issues like interfacial debonding, material property degradation, and barrel distortion, which can impact the accuracy, reliability, and service life of the firearm. This review provides an overview of the mathematical methods used to analyse thermal stresses in multilayered composite gun barrels. It examines the theoretical foundations of heat transfer and thermoelasticity, exploring both analytical and numerical techniques for modelling and predicting thermal stress distributions. Additionally, the review investigates the influence of key factors, such as material properties, layer geometry, and firing conditions, on the overall thermal response. This review aims to equip engineers and researchers with the knowledge to design and optimize high-performance, durable firearm systems.

Keywords: Multilayered composite, Gun barrel, Thermal stress analysis, Mathematical methods.

Introduction

The relentless pursuit of enhanced performance in firearm technology has led to the exploration of advanced materials and manufacturing techniques. Multilayered composite gun barrels have emerged as a promising alternative to traditional monolithic barrels, offering a unique combination of lightweight construction, high-rate-of-fire capability, and extended barrel life [1] [2]. These barrels, typically constructed by alternating layers of metallic and composite materials, leverage the desirable properties of each material to achieve superior performance characteristics [3]. However, the design and analysis of these complex structures necessitate a deep understanding of the intricate interplay between heat transfer, material behaviour, and structural integrity.

The advantages of multilayered composite gun barrels are multifaceted. Their enhanced strength-to-weight ratio, achieved by incorporating high-strength composite materials, allows for weight reduction without compromising structural integrity [4] [5]. This is crucial for improving weapon manoeuvrability and portability, particularly in large-caliber systems like the M256 120-mm cannon [2]. Additionally, the lower thermal conductivity of composite materials compared to metals enables efficient heat dissipation, reducing thermal distortions and improving accuracy during sustained firing [3] [4] [6]. Furthermore, the inherent corrosion resistance of composite materials extends barrel life and reduces maintenance requirements, particularly in harsh environments [1] [5].

Despite these advantages, the design and analysis of multilayered composite gun barrels present unique challenges. The bonding of dissimilar materials with different thermal expansion coefficients introduces interfaces that can significantly influence the barrel's mechanical and thermal behaviour [4]. The extreme temperatures and dynamic loading during firing generate significant thermal stresses, which, if not properly accounted for, can lead to interfacial debonding, material degradation, and ultimately, catastrophic failure [6] [3].

The extreme temperatures generated during firing present a significant challenge in the design of large-caliber gun barrels [7]. The rapid heating and cooling cycles, coupled with high pressures, induce substantial thermal stresses within the barrel structure. To accurately predict and mitigate these stresses, researchers have focused on developing sophisticated analytical and numerical models [8]. These models often involve inverse heat transfer techniques to estimate the heat flux and temperature distribution within the barrel wall using experimentally measured data [9]. By understanding the thermal behaviour of the barrel, engineers can optimize its design, material selection, and manufacturing processes to enhance its performance, durability, and service life.

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The intense heat generated during firing, particularly in rapid-fire scenarios, poses a significant challenge to maintaining the structural integrity and performance of gun barrels [10]. This heat, primarily originating from the combustion of propellant charges [11], can lead to elevated temperatures within the barrel, potentially exceeding critical thresholds and compromising material properties [12].

Furthermore, the presence of thermal contact resistance between different layers in a multilayered barrel, such as a steel cylinder and chrome coating, can exacerbate thermal stress concentrations [13]. Understanding and mitigating these thermal effects is crucial for ensuring the reliability and longevity of gun barrels under demanding operating conditions.

The quest for enhancing the lifespan and performance of gun barrels under high temperatures and pressures has driven significant research into advanced material applications and cooling techniques. One such advancement is the use of tantalum coatings, known for their high melting point and wear resistance [14]. However, the interface between the coating and the underlying steel substrate becomes a critical area of concern, as thermal stresses can induce shear damage and potentially compromise the barrel's integrity [15]. To address this, researchers are exploring innovative cooling methods, such as composite cooling channels integrated into the barrel structure, to effectively manage heat dissipation during firing [16]. These advancements, coupled with a deeper understanding of the thermo-mechanical behavior of propellants during combustion [17], are paving the way for the development of more resilient and reliable gun barrel systems.

Accurately modelling and predicting the thermal behaviour of a gun barrel during firing is crucial for understanding wear patterns, potential cook-off risks, and overall barrel life [18]. This task, however, is complex due to the transient nature of heat transfer during the ballistic cycle and the intricate geometries involved. Researchers are increasingly turning to numerical simulations, validated by experimental data [19], to gain deeper insights into these processes. Advanced techniques, such as inverse heat flux reconstruction [20], are being employed to estimate the heat loads experienced by the barrel based on temperature measurements, providing valuable data for optimizing barrel design and material selection for improved performance and durability.

This review delves into the mathematical methods employed in the thermal stress analysis of multilayered composite gun barrels. It examines the fundamental principles governing heat transfer, material behaviour, and structural mechanics in these complex systems. By understanding these principles and the associated mathematical frameworks, engineers can effectively design and analyse multilayered composite gun barrels that meet the demanding performance requirements of modern weaponry.

Thermal Stresses in Multilayered Composite Gun Barrels

The analysis of thermal stresses in multilayered composite gun barrels begins with the understanding of heat transfer within these structures. During the firing of a gun, the barrel is subjected to intense heat flux from the propellant combustion, resulting in significant temperature gradients along the barrel's length and through its thickness. These steep thermal gradients, coupled with the mismatch in

thermal expansion coefficients between the metallic and composite layers, give rise to thermal stresses that can significantly impact the barrel's structural integrity.

To model the thermal stress behaviour of multilayered composite gun barrels, researchers have employed a range of analytical and numerical techniques. Analytical approaches, such as the classical lamination theory and the Timoshenko beam theory, provide closed-form solutions for the temperature distribution and associated thermal stresses. These methods rely on simplifying assumptions, such as plane stress or plane strain conditions, and enable a deeper understanding of the underlying mechanisms governing the thermal response of the barrel.

Numerical techniques, on the other hand, offer greater flexibility in accommodating complex geometries, material properties, and boundary conditions. Finite element analysis has become a widely adopted tool for the thermal stress analysis of multilayered composite gun barrels. These models can capture the intricate interactions between the various layers, including the effects of interfacial contact resistance and the non-linear behaviour of materials at elevated temperatures.

The thermal stress analysis of multilayered composite gun barrels must also account for the dynamic loading conditions experienced during firing. The rapid pressure and temperature rise, coupled with the inertial effects of the projectile, can induce significant transient stresses that may exceed the material's strength, leading to potential failure modes such as layer delamination or matrix cracking. Researchers have employed advanced computational techniques, such as fluid-structure interaction and coupled thermal-structural analysis, to accurately model these complex, time-dependent phenomena.

Contact Resistance and Thermal Stresses

The presence of contact resistance at the interfaces between the metallic and composite layers in a multilayered gun barrel can significantly impact the thermal stress distribution. Contact resistance arises due to the imperfect bonding between the materials, resulting in a localized temperature jump at the interface. This temperature discontinuity, in turn, alters the thermal gradient and the associated thermal stresses within the barrel.

To account for the effects of contact resistance, researchers have developed sophisticated mathematical models that incorporate thermal contact conductance at the material interfaces. These models often rely on empirical correlations or experimental data to estimate the contact resistance, which can vary depending on factors such as surface roughness, contact pressure, and temperature.

The inclusion of contact resistance in the thermal stress analysis of multilayered composite gun barrels is crucial for accurately predicting the barrel's performance and reliability. Neglecting the contact resistance can lead to underestimation of the thermal stresses, particularly at the interfaces, potentially resulting in premature failure of the barrel during service.

Material Properties:

In addition to the influence of thermal contact behaviour, the accurate characterization of material properties, particularly at elevated temperatures, is crucial for the thermal stress analysis of multilayered composite gun barrels. The thermal and mechanical properties of both the metallic and composite constituents, including thermal conductivity, coefficient of thermal expansion, specific heat, and tensile/compressive strength, can exhibit significant temperature dependence. This temperature-dependent material behaviour can significantly impact the heat transfer and stress distribution within the barrel, necessitating its accurate representation in the thermal stress models. Advanced experimental methods, such as high-temperature testing, thermogravimetric analysis, and differential scanning calorimetry, have been employed to obtain reliable, temperature-dependent material property data for use in the thermal stress analysis of these complex multilayered structures.

Failure Analysis:

The thermal stress analysis of multilayered composite gun barrels must also consider the potential for various failure modes, such as interfacial debonding, matrix cracking, and fiber breakage. Researchers have developed comprehensive, theoretically-grounded failure criteria, based on both stress-based and energy-based approaches, to predict the onset of these critical failure mechanisms. These failure criteria, which account for the intricate interplay of thermal stresses, material properties, and structural interactions, provide crucial insights to guide the design and optimization of the barrel's layered architecture. By incorporating these advanced failure analysis techniques, engineers can work to ensure the structural integrity and reliability of multilayered composite gun barrels under the demanding operating conditions encountered during firing.

Discussion:

The thermal stress analysis of multilayered composite gun barrels is a complex and multifaceted field that requires a deep understanding of heat transfer, material behaviour, and structural mechanics. By leveraging analytical and numerical techniques, researchers have made significant strides in modelling the intricate thermal and mechanical interactions within these systems, including the critical effects of contact resistance at the material interfaces. The accurate prediction of thermal stresses is essential for

the design and optimization of high-performance multilayered composite gun barrels, ensuring their reliability and service life under the demanding operating conditions encountered in the firing of modern firearms. This comprehensive understanding of the thermal stress behaviour of these complex structures is crucial for improving the overall performance, safety, and reliability of advanced composite gun barrels used in various military and defence applications.

Conclusion:

Thermal stress analysis is a crucial aspect of the design and development of multilayered composite gun barrels. By combining advanced analytical and sophisticated numerical techniques, researchers have gained a deeper and more comprehensive understanding of the complex thermal and mechanical phenomena governing the barrel's performance, including the significant impact of contact resistance at the material interfaces. The accurate characterization and thorough investigation of temperature-dependent material properties, as well as the consideration of potential failure modes such as interfacial debonding, matrix cracking, and fibre breakage, are essential for the reliable prediction of thermal stresses and the optimization of the barrel's layered structure. This holistic approach to thermal stress analysis is crucial for improving the overall performance, safety, and reliability of advanced composite gun barrels used in various military and defence applications.

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References

- [1] M. Zieliński, P. Koniorczyk, Z. Surma, M. Preiskorn and J. Sienkiewicz, "Selected Aspects of Heat Transfer Study in a Gun Barrel of an Anti-Aircraft Cannon", Problems of Mechatronics Armament, Aviation, Safety Engineering, Vol. 14 (2), 73-86, 2023.
- [2] Joseph T. South and Robert H. Carter, "Thermal Analysis of an M256 120-mm Cannon", U.S. Army Research Laboratory, 2005.
- [3] A. Şentürk, H. Işık and C. Evcı, "Thermo-mechanically coupled thermal and stress analysis of interior ballistics problem", International Journal of Thermal Sciences, Vol. 104, 39-53, 2016.

- [4] Chen Longmiao, Qian Linfang, and Xu Yadong, "Numerical simulation of transient thermal response of composite material barrel during gun firing", 2008 Asia Simulation Conference -7th Intl. Conf. on Sys. Simulation and Scientific Computing, 633-637, 2008.
- [5] X. Dong, X. Rui, C. Li, Y. Wang and L. Fan, "A calculation method of interior ballistic two-phase flow considering the recoil of gun barrel", Applied Thermal Engineering, Vol. 185 ,116239, 2021.
- [6] T. Nguyen, M. P. Nguyen and H. T. Lai, "Determination the Stress and Deformation of the Cannon Barrel when Fired", Engineering and Technology Journal, Vol. 08, 2887-2897, 2023.
- [7] P. Qu, Q. Li and S. Yang, "Temperature Field and Thermal Stress Analysis of Large Caliber Gun Barrel", Applied Mechanics and Materials, Vol. 518, 150-154, 2014.
- [8] Haw-Long Lee, Yu-Ching Yang, Win-Jin Chang, and Tser-Son Wu, "Estimation of heat flux and thermal stresses in multilayer gun barrel with thermal contact resistance", Applied Mathematics and Computation Vol. 209, 211–221, 2009.
- [9] Tsung-Chien Chen a, Chiun-Chien Liu, Horng-Yuan Jang, and Pan-Chio Tuan, "Inverse estimation of heat flux and temperature in multi-layer gun barrel", International Journal of Heat and Mass Transfer Vol. 50,2060–2068, 2007.
- [10] M. Ghanem, O. Abdelsalam, S. Guirgis and M. A. Khair, "Solution of Heat Transfer Problem for Thick-Walled Automatic Weapon Barrel Subjected to Continuous Firing", 17th International Conference on Aerospace Sciences & Aviation Technology, 2017.
- [11] Ercan Degirmenci, Celal Evci, Halil Isık, Mehmet Macar, Nadir Yılmaz, M. Hüsnu Dirikolu, and Veli Çelik, "Thermo-mechanical analysis of double base propellant combustion in a barrel", Applied Thermal Engineering, Vol. 102,1287–1299, 2016.
- [12] Bin Wu, Gang Chen, and Wei Xia, "Heat transfer in a 155 mm compound gun barrel with full length integral midwall cooling channels", Applied Thermal Engineering, Vol. 28, 881–888, 2008.
- [13] Yu-Ching Yang, Haw-Long Lee, Jung-Chang Hsu, and Shao-Shu Chu, "Thermal Stresses in Multilayer Gun Barrel with Interlayer Thermal Contact Resistance", Journal of Thermal Stresses, Vol. 31, 624–637, 2008.
- [14] S. Y. Chen, L. M. Chen, J. Fu and Y. Z. Li, "Heat Transfer Analysis of the Tantalum-plated Barrel", Journal of Physics: Conference Series, 2460, 012087, 2023.

- [15] X. Li, Y. Zang, Y. Lian, M. Ma, L. Mu and Q. Qin, "An interface shear damage model of chromium coating/steel substrate under thermal erosion load", *Defence Technology*, Vol.17, 405-415, 2021.
- [16] X. Liu, D. Wu and J. Hou, "Numerical Analysis of 100mm Naval Gun Barrel Composite Cooling Based on Multiphase Flow", *Engineering Letters*, Vol.28(3),2020.
- [17] C. Evcil, and H. Işık, "Analysis of The Effect of Propellant Temperature on Interior Ballistics Problem", *Journal of Thermal Engineering*, Vol. 4, Special Issue 8, 2127-2136, 2018.
- [18] Ç. Susantez and A. B. Caldeira, "Heat Transfer Modelling and Simulation of a 120 mm Smoothbore Gun Barrel During Interior Ballistics", *Defence Science Journal*, Vol. 72, 30-39, 2022.
- [19] K. A. Suyadnya, D. Tarwidi, E. B. Setiawan and R. F. Umbara, "Numerical Modeling of Heat Transfer in Gun Barrel with Experimental Validation", *International Journal of Engineering & Technology*, Vol. 8, 62-66, 2019.
- [20] S. Chen, L. M. Chen, J. Fu and Y. J. Li, "Reconstruction of the heat flux input of coated gun barrel with the interfacial thermal resistance", *Case Studies in Thermal Engineering*, Vol. 49, 103242, 2023.