

# A novel secure group RFID authentication protocol

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## Abstract

The trend of researching group radio frequency identification devices (RFID) authentication protocol has become increasingly popular in recent years. One of the newest work in this area is from Batina and Lee, they presented a privacy-preserving multi-players grouping-proof protocol based on the elliptic curve cryptography (ECC), and claimed their protocol have the ability to resist five potential attacks, including compromised tag attack, man-in-the-middle attack, colluding tags attack, etc.

In this paper, we first take a counterexample to demonstrate their protocol is vulnerable to compromised tag attack. Then we propose a novel secure RFID authentication protocol, and analyze its security by merging formal analysis, provable security, and mathematical inductive method, so as to solve the weakness of Batina and Lee's work. Furthermore, compared with another two classic protocols (secure ownership transfer protocol (SOTP) and secure multiple group ownership transfer protocol (SMGOTP)), the performance analysis show that our protocol provides not only a lower tags' communication cost at about 50.0% and 14.3%, but also a lower reader's computation cost (approximate 14.5% and 55.1% respectively), when transferring a large number of tags.

**Keywords** group RFID authentication, compromised attack, elliptic curve, RFID, internet of things (IOT)

## 1 Introduction

Radio frequency identification devices (RFID) is the most common perception technique of IOT. It applies radio signals to automatically and uniquely identifies objects, has been widely applied in several important areas nowadays, such as Logistics Industry, Retailing, Apparel Industry, Asset Management, Identity Recognition, E-Business, etc. To be specific, RFID handheld devices are used to identify the information of identity (ID), and then the real-time information about the state of the corresponding objects or the surrounding environment can be transferred rapidly via 3G networks. It is generally used primarily for mobile enforcement of the policemen, traffic police and border armed police. There are practical scenarios where grouping-proofs could meaningful develop the capabilities of RFID-based systems [1]. For instance, (1) pharmaceutical sector could check a medicine

which is sold joined with its prescription or with its information leaflet; (2) government paperwork could verify a single form which is enclosed with its corresponding stamp or label; (3) meetings or access control systems could generate a kind of evidence which a group of people are present at a specific location. (4) airport check-in desks could link your boarding card with your passport and baggage. Nevertheless, all sorts of security threats reported have been growing dramatically over the past several years. No doubt that authentication of RFID is the essence to tackle with the potential risks.

In fact, after the experiences with six decades from its invention, scientific research about the security of RFID has mainly concentrated on the function of authentication between one or two tags and a reader, such as Park and Hur [2] and Sadighian and Jalili [3]. However, group RFID authentication protocols remain have not been lucubrate until Batina and Lee [4]. More specially, Batina and Lee [4] extended the notion of RFID authentication protocol to the public-key cryptography, and proposed a privacy-preserving multi-players grouping-proof protocol which is

exclusively dependent on the use of ECC.

After that, a large body of work concentrated on the topic of group RFID technology in recent years [5–12]. Sato and Mitsugi [13] proposed a group verification method, named ‘group coding’, which verified the integrity of a group of tags without a network connection. The ‘group coding’ could be aware of the number of RFID tags missing from the group when the group was attacked. But they cannot take any potential attacks into account. Fornaciari and Cucchiara [14] proposed a camera and RFID subtly mingle method which can hamper attacker to location in a real noisy and complex wide environment. Their method can address uncertain data and manage conflicts which combines from the two sources, thus they refrain from some potential intruders. Yang [15] proposed a secure multiple group ownership transfer protocol, which can perform ownership transfer across different authorities and achieve mutual authentication among tags, the reader and the verifier. They claimed that their protocol is able to prevent from replaying attack, eavesdropping and message modification, although not including compromised tag attack.

Our main contributions can be summarized as follow:

1) A novel secure group RFID authentication protocol is proposed.

2) The security of the proposed protocol is analyzed by merging formal analysis, provable security, and mathematical inductive method.

3) Compared with another two classic protocols (SOTP and SMGOTP), the performance analysis show that our protocol provides not only a lower tags’ communication cost at about 50% and 14.3%, but also a lower readers computation cost (approximate 14.5% and 55.1% respectively), when transferring a large number of tags.

This paper has been divided into the following sections: Sect. 2 presents the preliminaries; Sect. 3 provide a counterexample to state that the protocol in Ref. [4] cannot resist compromised tag attack; Sect. 4 presents the revised grouping proof protocol and proves its security; Sect. 5 carries out some experiments and analyzes the computation and communication loads with other two protocols. Finally, in Sect. 6 we show the conclusion.

## 2 Preliminaries

In this section, we first introduce ID-transfer scheme. Before introducing the definition, we will introduce the

notation used in this work. We denote  $P$  as the base point on an elliptic curve,  $y$  and  $Y = yP$  are the trusted verifier’s private key and public key pair, where  $yP$  denotes the point derived by the point multiplication operation on the elliptic curve group. We let the notation  $x(T)$  to denote the  $x$ -coordinate of the point  $T$  on the elliptic curve. The values  $s_t$  and  $S_t (= s_tP)$  are the private key and public key pair of tag  $t$ . One point should note, although the name suggests that it can be publicly known, that a tag should not reveal its public key during the execution of the protocol, as this would cause tracking attacks [16].

### Definition 1 ID-Transfer scheme [16]

The ID-transfer scheme of elliptic curve based randomized access control (EC-RAC) is shown in Fig. 1. In this scheme, a tag firstly chooses a random value  $r_{t1} \in_R Z$ , and then computes  $T_1 = r_{t1}P$ . After that, it sends  $T_1$  to the reader. Then, the reader responds with a random challenge  $r_{s1} \in_R Z$ . Hence, the tag produces  $T_2 = (r_{t1} + r_{s1}x_1)Y$  by using its own private key  $x_1$  and sends the message  $T_2$  to the reader. Upon receipt of message  $T_2$ , the reader sends it to the verifier in an secure network environment. The verifier calculates  $x_1P (= X_1) = (y^{-1}T_2 - T_1)r_{s1}^{-1}$ , which is used to check whether the corresponding tag is registered in the reader.

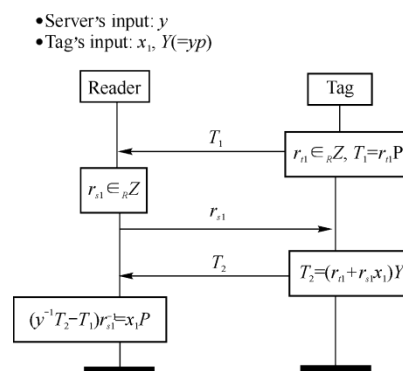


Fig. 1 ID-Transfer Scheme

Here, we recall the definition of the ECC-based grouping-proof protocol with colluding tag prevention. The main idea of ECC-based grouping-proof protocol is to intermingle runs of the ID-transfer protocol with multiple tags into a single grouping-proof protocol which denotes as the colluding tag prevention (CTP) protocol [4].

### Definition 2 ECC-based grouping-proof protocol

The 2-party CTP protocol, which allows a couple of

RFID tags (denoted by tag  $A$  and  $B$ ) to illustrate that they have been scanned simultaneously, is shown in Fig. 2. Note that we assume that the underlying communication protocol is able to detect and solve collisions. During the entire execution of the protocol, tags or the reader abort when a timeout occurs, when they receive the EC point at infinity, or when they receive an EC point with its  $x$ -coordinate equal to zero or the order of the point  $P$  on the curve. The protocol works as follows. The reader first sends the messages ‘start left’ and ‘start right’ to indicate the role of the tags in the protocol. Next, tag  $A$  chooses a random number  $r_a$  and computes the corresponding EC point  $T_{a,1} = r_a P$ . The reader generates  $r_s \in_R Z$ , and then forwards it to tag  $B$ . Upon receipt of  $T_{a,1}$ , tag  $B$  will first choose a random number  $r_b$  and compute the corresponding message  $T_{b,1} = r_b P$ . Next, it also computes the response  $T_{b,2} = [r_b + x(r_s T_{a,1}) s_b] Y$  using its private key  $s_b$ , the random number  $r_b$ , the  $x$ -coordinate of the challenge  $T_{a,1}$ , and a random challenge  $r_s$  generated by the reader. Both  $T_{b,1}$  and  $T_{b,2}$  are handed down to the reader. In the next phase of the protocol, the reader forwards  $T_{b,2}$  to tag  $A$ . This tag will compute the response  $T_{a,2} = [r_a + x(T_{b,2}) s_a] Y$  using its private key  $s_a$ , the random number  $r_a$  and the  $x$ -coordinate of challenge  $T_{b,2}$ . The result is forwarded to the reader. The grouping proof, collected by the reader, consists of the following tuple:  $(T_{a,1}, T_{a,2}, r_s, T_{b,1}, T_{b,2})$ .

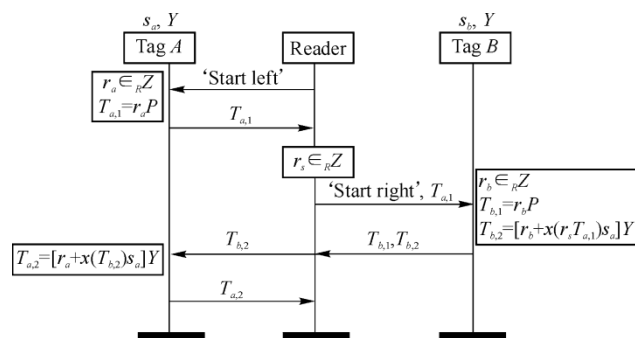


Fig. 2 Two-party grouping proof protocol with CTP

To verify the grouping-proof protocol constructed by tag  $A$  and  $B$ , the verifier will accomplish the following computations:

$$s_a P = (y^{-1} T_{a,2} - T_{a,1}) [x(T_{b,2})]^{-1}$$

$$s_b P = (y^{-1} T_{b,2} - T_{b,1}) [x(r_s T_{a,1})]^{-1}$$

Note that this does not require an exhaustive search

through a database with all known public keys, but rather uses the verifier’s secret key  $y$  to compute these public keys from the proof. If the public keys of tag  $A$  and  $B$  ( $S_a$  and  $S_b$ , respectively) are registered in the database of the verifier, the grouping proof is accepted and the timestamp is added. Otherwise, the proof is not accepted and the timestamp is not added [4]. The two-party CTP grouping-proof protocol can be easily extended to multipletags.

### 3 Compromised tag attack

A novel extended ECC-based RFID authentication protocol is shown, which can resist against compromised tag attack. However, we found that a compromised tag attack can be carried out on the adversarial model. We describe it as shown in Fig. 3.

The 2-party CTP protocol allows a pair of RFID tags (denoted by tag  $A$  and  $B$ ) to prove that they have been scanned simultaneously. The protocol works as follows.

First of all, we describe a session (denote as  $S_1$  in the Fig. 3): the reader sends the message ‘start left’ to the tag  $A$ . Upon receipt of the message ‘start left’ from the reader, tag  $A$  chooses a random value  $r_a \in_R Z$ , and then computes  $T_{a,1} = r_a P$ . After that it sends  $T_{a,1}$  to the reader. Upon receipt of the message  $T_{a,1}$ , the reader chooses a random

value  $r_s \in_R Z$  and the corresponding EC point  $T_{a,1}$ . This message is then forwarded to Tag  $B$ . At this time, this session  $S_1$  isn’t completed. Then we start another session (denote as  $S_2$  in the Fig. 3). An attacker can resend the set of messages  $r_a \in_R Z$ ,  $T_{a,1} = r_a P$ , which has been received from  $S_1$ , to the reader. The reader chooses a random value  $r'_s \in_R Z$  and the corresponding EC point  $T_{a,1}$ . At this time, the attacker corrupts the tag  $B$ , sets  $r_b = x(r'_s T_{a,1}) s_b$ , computes  $T_{b,1} = r_b P$ , and  $T_{b,2} = [r_b + x(r_s T_{a,1}) s_b] Y$ , then  $T_{b,1}$ ,  $T_{b,2}$  is forwarded to the reader. After that, the reader forwards the message  $T_{b,2}$  to tag  $A$ . Upon receipt of the message  $T_{b,2}$ , tag  $A$  computes  $T_{a,2} = [r_a + x(T_{b,2}) s_a] Y$  via the private key  $s_a$ . After that the message  $T_{a,2}$  is sent to the reader. Later on, the verifier performs the following computations:

$$s_a P = (y^{-1} T_{a,2} - T_{a,1}) [x(T_{b,2})]^{-1}$$

$$s_b P = (y^{-1} T_{b,2} - T_{b,1}) [x(r_s T_{a,1})]^{-1}$$

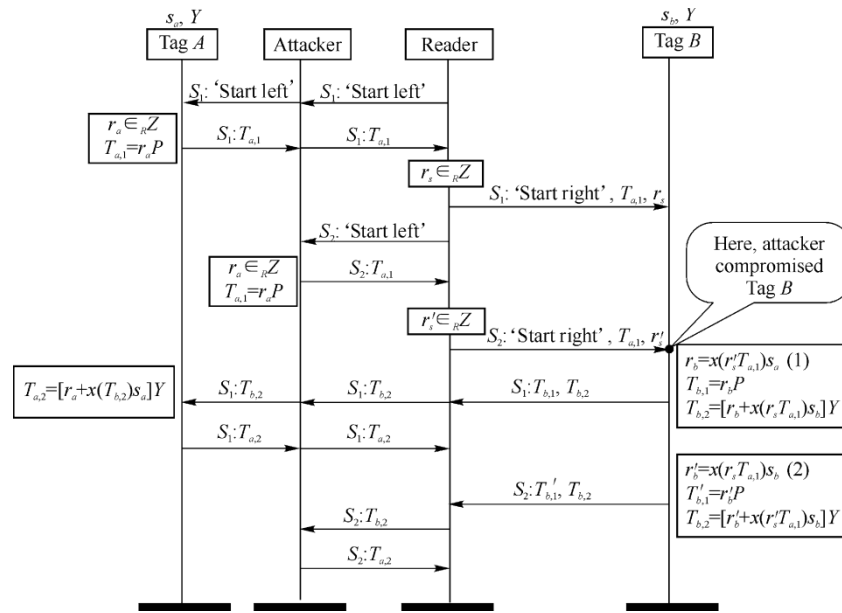


Fig. 3 Compromised Tag on the 2-party grouping proof protocol with CTP

Here we complete the  $S_1$  by now.

Secondly, the attacker sets  $r'_b = x(r'_s T_{a,1})s_b$ ,  $T'_{b,1} = r'_b P$  and  $T_{b,2} = [r'_b + x(r'_s T_{a,1})s_b]Y$ , and then sends  $T'_{b,1}$ ,  $T_{b,2}$  to the reader. When the reader forwards the message  $T_{b,2}$  to tag A, the attacker makes use of the message  $T_{a,2}$ , which sent in the  $S_1$ , to forward the message to the reader.

At last, the verifier performs the following computations:

$$s_a P = (y^{-1}T_{a,2} - T_{a,1})[x(T_{b,2})]^{-1}$$

$$s_b P = (y^{-1}T_{b,2} - T_{b,1})[x(r'_s T_{a,1})]^{-1}$$

By checking, the reader can accept the forged message which utilized the eavesdropped messages during the previous session in  $S_1$ . If the public keys of A and B are registered in the database of the reader, the grouping proof is accepted and a timestamp is added.

#### 4 The novel secure grouping-proof protocol against compromised tag attack

Due to the compromised tag attack described in the Sect. 3, we construct a novel extended two-party grouping proof protocol with CTP which solve the weakness of the original ECC-based RFID authentication protocol. Firstly, we introduce the new scheme, which is shown in Fig. 4.

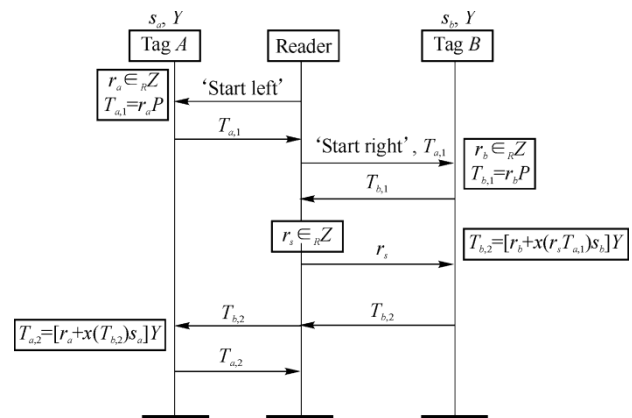


Fig. 4 The revised 2-party grouping-proof protocol against compromised tag attack

##### Scheme description

In the new scheme, the reader sends the message ‘start left’ to tag A. Upon receipt of the message ‘start left’ from the reader, tag A chooses a random value  $r_a \in_R Z$ , and computes  $T_{a,1} = r_a P$ , after that it sends  $T_{a,1} = r_a P$  to the reader. Upon receipt of the message  $T_{a,1}$ , the reader forwards it and the message ‘start right’ to the tag B. When tag B receives the message from the reader, it chooses a random value  $r_b \in_R Z$  and generates  $T_{b,1} = r_b P$ , then the message  $T_{b,1}$  is sent back to the reader. Once receiving the message, the reader chooses a random value  $r_s \in_R Z$  and sends the message  $r_s$  to the tag B. When receiving

the message from the reader, tag  $B$  utilizes its private key  $s_b$  to compute  $T_{b,2} = [r_b + x(r_s T_{a,1})s_b]Y$ . The message  $T_{b,2}$  is sent to the reader, and the reader forwards the message to tag  $A$ . Once receipt of the message  $T_{b,2}$ , tag  $A$  will use its own private key  $s_a$  to compute  $T_{a,2} = [r_a + x(T_{b,2})s_a]Y$ , and then send this  $T_{a,2}$  to the reader. The verifier performs the following computations:

$$s_a P = (y^{-1}T_{a,2} - T_{a,1})[x(T_{b,2})]^{-1}$$

$$s_b P = (y^{-1}T_{b,2} - T_{b,1})[x(r_s T_{a,1})]^{-1}$$

and checks it whether correct or not.

### Security analysis

Intuitively, we consider that the 2-party grouping proof protocol is secure.

It's trivial to find that the protocol shown in Fig. 2 does not consider resistance to compromised tag attack. As an illustration, we construct the scheme shown above which can avoid the defection of two-party grouping-proof protocol. Owing to the message  $r_s \in_R Z$  generated by the reader between the message  $T_{b,1}$  and  $T_{b,2}$ , and therefore, in the revised scheme, we can solve the problem of the compromised tag attack. More specifically, when the attacker computes the message  $r_b$ , the message  $r_s'$  must be fixed in prior based on Eq. (1) in Fig. 3. This leads that  $r_b'$  must have been set based on the specification of the revised scheme as in Eq. (2) in Fig. 3. Since  $r_b'$  is computed by  $r_s$ , the reader must have chosen the value  $r_s \in_R Z$ , which means that  $r_b$  has been fixed before. This paradox illustrates that the attack we found in Fig. 3 did not exist, thus our scheme avert this kind of attack.

Three-party grouping-proof isn't exactly the same as two-party grouping proof, we will illustrate it (constructed by tags  $A, B$  and  $C$ ). In this case, the message  $T_{b,2}$  is sent to tag  $C$  rather than the reader. Upon receipt of the message, tag  $C$  will choose a random value  $r_c \in_R Z$  and perform the following two computations:  $T_{c,1} = r_c P$ ,  $T_{c,2} = [r_c + x(T_{b,2})s_c]Y$ . The outcome  $T_{c,1}$ ,  $T_{c,2}$  are sent back to the reader, which forwards  $T_{c,2}$  to the tag  $A$ . Once tag  $A$  receipt of the message  $T_{c,2}$ , it uses its own private key  $s_a$  to compute  $T_{a,2} = [r_a + x(T_{c,2})s_a]Y$ , and then sends this  $T_{a,2}$  to the reader. For the sake of validating correctness, the verifier needs to compute the following

computations:

$$s_a P = (y^{-1}T_{a,2} - T_{a,1})[x(T_{c,2})]^{-1}$$

$$s_b P = (y^{-1}T_{b,2} - T_{b,1})[x(r_s T_{a,1})]^{-1}$$

$$s_c P = (y^{-1}T_{c,2} - T_{c,1})[x(T_{b,2})]^{-1}$$

By computing, the verifier can verdict whether the identifications of all the tags are the parties which the reader intend to communicate with or not. (See the rigorously prove farther below)

First of all, we are about to introduce the formalized definition of the grouping-proof protocol with CTP.

**Definition 3** The implementation of grouping-proof protocol with CTP

To begin with, we will list the notations used in the following definitions. Since reader and verifier communications are through a secured channel, we will only discuss the transmittal messages among the reader and all the tags. The notations used in our definition are listed in Table 1.

**Table 1** Notation used in the definition

Notations	Explanation for Notations
$i \in_R Z$	The number of the tags
$p_i$	The $i$ th tag among all the tags
$P$	The base point in an elliptic curve
$y$	The trusted verifier's private key
$Y (= yP)$	The trusted verifier's public key
$T$	The point on the elliptic curve
$x(T)$	The $x$ -coordinate of the point $T$
$s_i$	The $i$ th tag's private key
$S_i (= s_i P)$	The $i$ th tag's public key, which equals to the point multiplication operation $S_i$ and the base point $P$

It's assumed that all tags are denoted as  $p_i, (i \in_R Z)$ , which are logically ordered like a cycle. One point should note, each  $p_i$  cannot reveal its own public key during the execution of the protocol. Steps of protocol to perform in the formalized way are as follows:

**Step 1** In round  $i, (i=1)$ , the reader sends the message 'start left' to the tag  $p_i$ . Tag  $p_i$  chooses a random value  $r_i \in_R Z$  and computes  $T_{i,1} = r_i P$ , and then sends  $T_{i,1}$  back to the reader.

**Step 2** In round  $i, (i=2)$ , upon receipt of  $T_{i-1,1}$ , the reader sends the messages 'start right' and  $T_{i-1,1}$  to the tag  $p_i$ . Once receipt of this message,  $p_i$  chooses a random value  $r_i$  and forwards  $T_{i,1} = r_i P$  back to the reader. When receiving this message, the reader will choose a random value  $r_s$  and send it to tag  $p_i$ . Tag  $p_i$  utilizes its own



private key  $s_i$  to compute  $T_{i,2} = [r_i + x(r_s T_{i-1,1})s_i]Y$  and forwards it to  $p_{i+1}$ .

**Step 3** In round  $i$ , ( $i=3, \dots, n-1$ ),  $p_i$  chooses a random value  $r_i$  and computes  $T_{i,1} = r_i P$ , and then utilizes its own private key  $s_i$  to compute

$T_{i,2} = [r_i + x(T_{i-1,2})s_i]Y$ , after that forwards it to tag  $p_{i+1}$ .

**Step 4** In round  $i$ , ( $i=n$ ),  $p_i$  chooses a random value  $r_i$  and forwards the message  $T_{i,1} = r_i P$  and  $T_{i,2} = [r_i + x(T_{i-1,2})s_{i-1}]Y$  to the reader. The reader receives these two messages, and then forwards  $T_{i,2}$  to tag  $p_{n-i+1}$ .

Tag  $p_{n-i+1}$  utilizes its own private key  $s_{n-i+1}$  to compute the message  $T_{n-i+1,2} = [r_{n-i+1} + x(T_{i,2})s_{n-i+1}]Y$ .

The verifier will check the correctness of the grouping-proof protocol by the following computations:

$$s_1 P = (y^{-1} T_{1,2} - T_{1,1}) [x(T_{1,2})]^{-1}$$

$$s_2 P = (y^{-1} T_{2,2} - T_{2,1}) [x(r_s T_{1,1})]^{-1}$$

$$s_i P = (y^{-1} T_{i,2} - T_{i,1}) p x(T_{i-1,2})^{-1}$$

where  $i = 3, \dots, n$ .

By computing, the verifier can verdict whether the identifications of all the tags are the participants that the reader intends to communicate with or not.

Secondly, we are about to prove that the 3-party grouping-proof protocol is secure.

**Lemma 1** 3-party grouping-proof protocol is secure.

**Proof** We analyze this 3-party grouping-proof protocol via the tool of ProVerif which utilizes the symbolic analysis approach. The specific description of algorithm named 3-party grouping-proof security (3-GPS) algorithm is proposed as follows:

**Algorithm** 3-GPS algorithm

(\* Secure channels \*)

free car.

free cbr.

free ccr.

free cbc.

(\* Free variables \*)

private free  $s_a$ .

private free  $s_b$ .

private free  $s_c$ .

private free  $y$ .

free  $S_a, S_b, S_c, Y, P, T_{b2}$ .

(\* Active adversary \*)

param attacker = active.

(\* Inverse function \*)

fun inver/1.

equation inver(inver(x)) = x.

(\* Add function \*)

fun add/2.

(\* Sub function \*)

fun sub/2.

(\* Multiply function \*)

fun multi/2.

(\* Get x-value function \*)

fun getx/1.

(\* Reduction equation \*)

reduc  $T_1(x, P) = \text{multi}(x, P)$ .

reduc  $T_2(x, y, z, w) = \text{multi}(\text{add}(z, \text{multi}(\text{getx}(x), y)), w)$ .

(\* The process \*)

let  $p_a = (\text{new } r_a; \text{in}(\text{car}, m_0);$

let  $T_{a1} = T(r_a, P)$  in out(car,  $T_{a1}$ ); in(car,  $m_1$ );

let  $T_{a2} = T_2(m_1, S_a, r_a, Y)$  in out(car,  $T_{a2}$ )).

let  $p_b = (\text{in}(\text{cbr}, m_2); \text{new } r_b;$

let  $T_{b1} = T_1(r_b, P)$  in out(cbr,  $T_{b1}$ ); in(cbr,  $m_3$ );

let  $T_{b2} = T_2(\text{multi}(m_3, m_2), S_b, r_b, Y)$  in out(cbc,  $T_{b2}$ )).

let  $p_c = (\text{new } r_c; \text{in}(\text{cbc}, m_4);$

let  $T_{c1} = T_1(r_c, P)$  in

let  $T_{c2} = T_2(m_4, S_c, r_c, Y)$  in out(ccr,  $(T_{c1}, T_{c2})$ ).

(new left; new right; out(car, left); in(car,  $m_5$ );

let  $T_{a1} = m_5$  in out(cbr,  $T_{a1}$ ); in(cbr,  $m_6$ ); let  $T_{b1} = m_6$  in;

new  $r_s$ ; out(cbr,  $r_s$ );

let  $(T_{c1}, T_{c2}) = m_7$  in

in(ccr,  $m_7$ ); out(car,  $T_{c2}$ ); in(car,  $m_8$ );

let  $T_{a2} = m_8$  in

out(car, choice[sP( $T_{c2}$ ,  $y$ ,  $T_{a2}$ ,  $T_{a1}$ ),

multi(sub(multi(inver(y),  $T_{a2}$ ),  $T_{a1}$ ),

inver(getx( $T_{c2}$ ))));

out(cbr, choice[sP(multi( $r_s$ ,  $T_{a1}$ ),  $y$ ,  $T_{b2}$ ,  $T_{b1}$ ),

multi(sub(multi(inver(y),  $T_{b2}$ ),  $T_{b1}$ ),

inver(getx(multi( $r_s$ ,  $T_{a1}$ ))));

out(ccr, choice[sP( $T_{b2}$ ,  $y$ ,  $T_{c2}$ ,  $T_{c1}$ ),

multi(sub(multi(inver(y),  $T_{c2}$ ),  $T_{c1}$ ),

inver(getx( $x$ )))]).

In this algorithm, we denote processes  $p_a$ ,  $p_b$ ,  $p_c$  and  $p_r$  as participants  $a$ ,  $b$ ,  $c$  and the reader  $r$  respectively. Each process can compute data, as well as sends and receives messages with others. We utilize operation choice ( $x, y$ ) to distinguish term  $x$  and  $y$ . If the result of choice is that observational equivalence is true, i.e.  $x$  and  $y$  is observational indistinguishable, then we can

illustrate that the protocol is secure. The result of the specific implementation is shown as follows.

```
-- Observational equivalence
Termination warning: v_282 <> v_283 & attacker2:v_281,
v_282 & attacker2:v_281,v_283 -> bad:
  Selecting 0
  Termination warning: v_285 <> v_286 & attacker2:v_285,
v_284 & attacker2:v_286,v_284 -> bad:
  Selecting 0
  Completing...
  Termination warning: v_282 <> v_283 & attacker2:v_281,
v_282 & attacker2:v_281,v_283 -> bad:
  Selecting 0
  Termination warning: v_285 <> v_286 &
attacker2:v_285,v_284 & attacker2:v_286,v_284 -> bad:
  Selecting 0
  200 rules inserted. The rule base contains 200 rules. 32 rules in
the queue.
  RESULT Observational equivalence is true (bad not derivable).
```

It implies that the 3-party grouping-proof protocol is secure. In other words, the output of this protocol success indicates that the result observational equivalence is true.

**Theorem 1**  $n$ -party ( $n > 2$ ) grouping-proof protocol is a secure protocol.

**Proof** By mathematical inductive method, we firstly prove that 3-party grouping proof protocol is secure. Secondly, assume that  $k$ -party grouping proof protocol is secure, then  $(k + 1)$ -party grouping-proof protocol is also secure.

3-party grouping-proof protocol has been proved in Lemma 1, thus we just need to prove the security of  $k$ -party grouping proof protocol. First of all, we utilize  $k$  tags' protocol  $\pi_k$  to simulate  $k + 1$  tags' protocol  $\pi_{k+1}$ . Assume to the contrary, if there is a  $k + 1$  tags' attacker  $\mathbb{C}_{k+1}$  against  $\pi_{k+1}$ , then there must exist  $k$  tags' attacker  $\mathbb{C}_k$  which against the protocol  $\pi_k$ .

Out of this attacker  $\mathbb{C}_k$ , we will run of  $\mathbb{C}_{k+1}$  by  $\mathbb{C}_k$ . The simple sketch will be given as follows.

1) Attacker  $\mathbb{C}_k$  performs protocol  $\pi_k$ , and it will obtain all the messages before tag A receives message which tag K sends. At this point,  $\mathbb{C}_k$  make the protocol temporarily halt.

2) Attacker  $\mathbb{C}_k$  simulates the  $(k + 1)$ th tag which participate in the protocol  $\pi_{k+1}$  and generates the private

key  $s_{k+1}$ .

3) Based on the private key, random values and the transfer message which tag  $A, B, \dots, K$  generate in the actual protocol, attacker  $\mathbb{C}_k$  creates a random value  $r_{k+1} = r_k + x(T_{k-1,2})s_k - x(T_{k,2})s_{k+1}$ .

4) Based on the messages  $r_{k+1}$  and  $T_{k,2}$ ,  $\mathbb{C}_k$  utilizes its own private key  $s_{k+1}$  to compute the message  $T_{k+1,2} = [r_{k+1} + x(T_{k,2})s_{k+1}]Y$ . In other words,  $\mathbb{C}_k$  runs of the attacker  $\mathbb{C}_{k+1}$  to simulate the protocol  $\pi_{k+1}$ . In line with the messages from step 2 and 3,  $\mathbb{C}_k$  responds the messages which  $\mathbb{C}_{k+1}$  should receive in the process during the execution of protocol  $\pi_{k+1}$ . After that, attacker  $\mathbb{C}_k$  sends the message  $T_{k+1,2}$  which equals to the message  $T_{k,2}$  to tag  $A_1$ . Upon receipt of the message  $T_{k+1,2}$ , tag  $A_1$  takes the message  $T_{k+1,2}$  as the message  $T_{k,2}$  to compute the value  $T_{1,2}$ , and then it sends this message to the reader.

The verifier could pass the validation.

Next, we detail the specific process of the simulation.

Assume that the order of the tags is exactly like  $p_1, p_2, \dots, p_i$  ( $\{p_i \mid i \in Z\}$ ) during the process of grouping-protocol performance. Values  $s_i$  and  $r_i$  are the tag  $p_i$ 's private key and random number pair. Let  $l$  be an upper bound on the number of these kinds of protocol which might be executed.

(a) Choose  $r \leftarrow^R \{1 \dots l\}$ .

(b) Invoke adversary  $\mathbb{C}_i$ , running the protocol interaction with parties  $p_i, (i \in Z_n)$ , just to obtain all the messages before tag  $p_1$  receives message which tag  $p_i$  sends. At this point,  $\mathbb{C}_i$  let the protocol temporarily halt.

(c) Adversary  $\mathbb{C}_{i+1}$  runs of the protocol with parties  $p_1, p_2, \dots, p_{i+1}$  normally. Invoke  $\mathbb{C}_i$  to simulate the  $(i + 1)$ th tag  $p_{k+1}$ , set  $r_{k+1} = r + x(T_{i-1,2})s_i - x(T_{i,2})s_{i+1}$ , for  $i \geq 3, i \in Z$ .  $s_{i+1}$  is the  $(i + 1)$ th tag's private key which generate by its own. Upon receipt of the message  $T_{i+1,2} = [r_{k+1} + x(T_{i,2})s_{i+1}]Y$ ,  $\mathbb{C}_i$  forwards it to  $\mathbb{C}_{i+1}$ , at this point, let  $\mathbb{C}_i$  send this message to tag  $p_1$ , which was halted in the step 2. Then, we make step 2 continue to run.

(d) Once receipt of the message  $T_{i+1,2}$ , tag  $p_1$  takes this message as the message which tag  $p_1$  sends. Out of  $T_{i+1,2}$  equals to  $T_{i,2}$ , tag  $p_1$  utilizes its own private key  $s_1$  to compute  $T_{1,2} = [r_1 + x(T_{i+1,2})s_1]Y$ , and then sends it to the reader. The verifier could pass the validation.

In this case, let  $q$  be a security parameter. We assume that the probability which attacker  $\mathcal{C}_{i+1}$  win the game with non-negligible probability. We have that:

$$\Pr[\mathcal{CE} = 1, q] = \frac{1}{i} \cdot \frac{1}{l(q)} \cdot \varepsilon(q)$$

$P_n^{i+1}$  denotes the probability of polynomial time for selecting  $i+1$  tags from  $n$  tags, among which the order of the  $i+1$  tags is fixed. And  $P_n^{i+1}$  is the polynomial of security parameter  $q$ . Let  $l$  be an upper bound on the number of these kinds of protocols which might be executed. And  $l$  is the polynomial concerning to security parameter  $q$ .  $\varepsilon(q)$  denotes non-negligible probability with security parameter  $q$ . And therefore, the probability which  $\mathcal{C}_i$  win this game is still a non-negligible  $\varepsilon(q)$  with respect to the security parameter  $q$ .

In conclusion,  $i$ -party grouping-proof protocol is secure, then  $(i+1)$ -party grouping proof protocol is also secure.

### 5 Performance analysis

First of all, we compare our proposed scheme with other three schemes in terms of the following aspects: resistance to replay attack (RA), resistance to denial of service (DoS) attack, resistance to man-in-middle (MiM) attack and resistance to compromised tag attack (CT). In Table 2, we use the notation ‘✓’ to denote functions achieved; and use the notation ‘✗’ to denote function not achieved. We obtain other protocols’ assumptions and their weaknesses from their researchers’ evaluation in their papers. Table 3 depicts that our protocol has the highest security than others, and it illustrates that our protocol can secure against all the RFID attacks which we mentioned above.

**Table 2** Comparison with other protocols

	RA	DoS	MiM	CT
BATINA [4]	✓	✓	✓	✗
SOTP [17]	✓	✓	✗	✗
SMGOTP [15]	✓	✓	✗	✗
OUR WORK	✓	✓	✓	✓

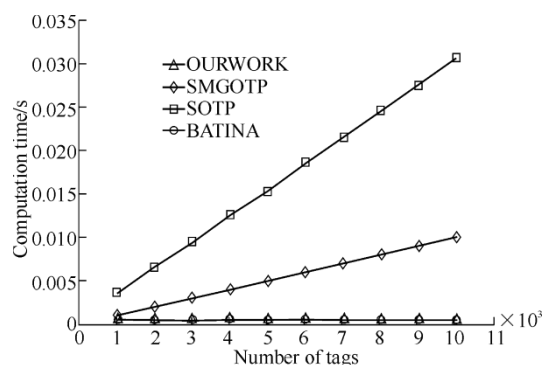
Next, we analyze the computation and communication loads of our protocol, and demonstrate that our scheme is feasible for the lightweight passive RFID tags. Hence, we compare our protocol with other three protocols and show their performances when transferring  $n$  tags in a group. The depicted and analyzed data of the three protocols are shown in the Table 3.  $T_{ran}$  denotes the time of choosing a random value;  $T_{ecc}$  denotes the time for elliptic curve operation;  $T_{lw}$  denotes the time for one lightweight

en/decryption;  $T_{en}$  denotes the time for one en/decryption;  $T_{rev}$  denotes the time for reversible operations. Since addition and subtraction operations require only a little computation, compared with multiplication and reversible operations, we leave them out in our performance analysis.

**Table 3** Computation loads and communication loads when transferring  $n$  tags

Schemes	Devices	Computation loads	Communication loads
BATINA [4]	Tag	$nT_{ran} + (2n+1)T_{ecc}$	$n+4$
	Reader	$T_{ran}$	
	Verifier	$(2n+1)T_{ecc} + T_{ran} + 2nT_{rev}$	
SOTP [17]	Tag	$3nT_{lw} + 2nT_{ran}$	$11n$
	Reader	$3nT_{en}$	
	Verifier	$9nT_{en} + 3nT_{lw} + 2nT_{ran}$	
SMGOTP [15]	Tag	$5nT_{lw}$	$2n+7$
	Reader	$(n+1)T_{en} + T_{ran}$	
	Verifier	$(n+9)T_{en} + (3n+2)T_{lw} + T_{ran}$	
OUR WORK	Tag	$nT_{ran} + (2n+1)T_{ecc}$	$n+6$
	Reader	$T_{ran}$	
	Verifier	$(2n+1)T_{ecc} + T_{ran} + 2nT_{rev}$	

We implement a simulation to display our performance comparison with other relevant schemes SOTP [17], SMGOTP [15] and Batina and Lee [4]. We mainly discuss three parts: the computation loads on tag’s part, the computation loads on the reader’s part and the communication loads on the reader’s part, are shown visually in Figs. 5–7.



**Fig. 5** Comparison of computation on reader’s part

In Fig. 5, we compare the computation loads with four protocols on reader’s part. Our protocol has the lowest computation time than the scheme SOTP [17] and SMGOTP [15], because the reader just needs to choose one random value during the whole protocol with all tags. We have almost the same computation loads as the scheme BATINA [4] in this part, and our scheme requires 50.0% computation loads of SOTP’s scheme and 14.3%



computation loads of SMGOTP's scheme.

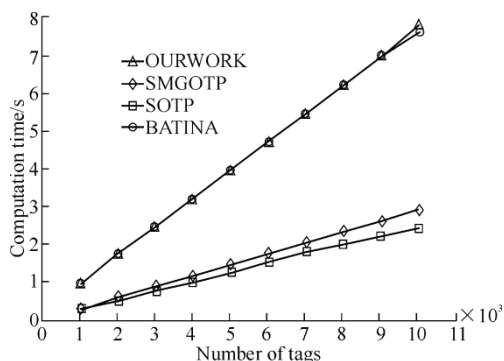


Fig. 6 Comparison of computation on Tags' part

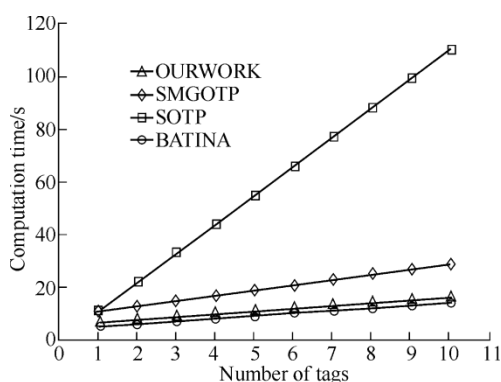


Fig. 7 Comparison of communication on Tags' part

We compare the computations with four protocols on tags' part. SMGOTP scheme requires three lightweight encryption algorithms, nevertheless our work and BATINA's need elliptic curve algorithms, see Fig. 6. Although our work has much higher computation time than their works, it's still acceptable. The implementation of our work is done with the thousands of tags. In addition, we have much higher security than other three schemes, is shown in Table 2.

We compare the communication loads with other three protocols on the tags' part, see shown in Fig. 7. The figure provide an illustration of communication loads, our scheme is clearly lower than the scheme SOTP and SMGOTP and have a slightly higher value than BATINA's. In this part, our scheme requires 14.5% communication loads of SOTP's, 55.1% communication loads of SMGOTP's and requires 14.3% higher communication loads than BATINA's.

## 6 Conclusions

A large number of RFID protocols which tags could be

scanned simultaneously have been proposed in recent years. Most of the protocols take man-in-the-middle attack into consideration, but they have not considered for the compromised tag attack. In this article, we find a kind of compromised tag attack in the two-party grouping proof protocols which compromise security. In view of this weakness, we propose a novel secure RFID authentication protocol which can avert this drawback. By formal analysis, provable security, and mathematical inductive method, we prove that our grouping-proof protocol with  $n$ -party ( $n \geq 3$ ) is secure and can resist against compromised tag attack. Finally, we provide some experimental analysis of the communication and computation loads. By analyzing, we found that our protocol provide a lower communication loads on the tags' part and has a lower computation loads on the reader's part than the protocols (SOTP and SMGOTP) when transferring a large number of tags. Although, our work has a much higher computation time than their works, it's still acceptable, because our protocol provide even more security than theirs.

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